Skills from previous math classes that you need to self-review for Math 1C

From Algebra:

Negative and fractional exponents Rational expressions Add / subtract Polynomial long division

From Trigonometry:

Sine / cosine / tangent of special angles on unit circle Inverse sine / cosine / tangent of special values Pythagorean / reciprocal / quotient / negative angle / co-function identities Double angle identity Trigonometric equations

From Precalculus:

Graphs of basic functions (domain, range, intercepts, asymptotes, long run behavior)

Power	$y = x^{n}$ (<i>n</i> could be positive or negative, even or odd or reciprocal of integer)									
Exponential	$y = b^x$ (<i>b</i> could be greater than or less than 1)									
Logarithmic	$y = \log_b x$ (<i>b</i> could be greater than or less than 1)									
Trigonometric	$y = \sin x$, $y = \cos x$, $y = \tan x$									
Parametric equations										
Graphs of basic conics										
Circles / ellipses / parabo	Circles / ellipses / parabolas / hyperbolas									
Symmetry of functions & graphs	(relationship between algebraic & graphical symmetry)									
Even / odd										
Sequences										
General formula										
Sigma notation for series										
Factorials										

From Calculus:

Limits (especially involving infinity) Continuity Derivatives (and their relationship to increasing/decreasing behavior of functions) Linear approximations L'Hospital's rule Anti-derivatives (basic, substitution, by parts) Improper integrals

<u>Unless stated otherwise, you must be able to solve these</u> <u>without your calculator</u>

[1] Find $81^{-\frac{3}{4}}$.

[2] Simplify
$$\frac{x^{-\frac{2}{3}}x^{\frac{3}{4}}}{x^{-\frac{1}{2}}}$$
.

- [3] Add and simplify $\frac{x-7}{x^2-4x+3} + \frac{x+7}{x^2-x-6}$.
- [4] Perform the long division $\frac{x^4 x^3 x^2}{x^2 + 2x + 5}$.
- [5] Determine algebraically if $f(x) = x\sqrt{1+x^2}$ is symmetric about the *y*-axis, about the origin or neither.
- [6] Determine algebraically if $f(x) = \sin x \cos x$ is even, odd or neither.

[7] Fill in the following table with all entries (in radians) that have exact values. Also, identify the entries which do not exist.

<i>x</i> =	$-\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{3}}{3}$	$-\frac{\sqrt{2}}{2}$	$-\sqrt{3}$	$-\frac{1}{2}$	-1	0	1	$\frac{1}{2}$	$\sqrt{3}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{3}$	$\frac{\sqrt{3}}{2}$
$\tan^{-1} x =$													
$\cos^{-1} x =$													
$\sin^{-1}x =$													

[8] Let $\theta = \frac{\pi}{6}$.

- [a] Find an angle with positive measure that is co-terminal with θ .
- [b] Find an angle with negative measure that is co-terminal with θ .
- [c] Find 3 angles between 0 and 2π that have θ as their reference angle, not including θ itself.

[9] State the following trigonometric identities.

- [a] the 3 Pythagorean identities that involve the 6 trigonometric functions
- [b] the co-function identities for each of the 6 trigonometric functions
- [c] the double angle identities for $\cos 2x$ (3 versions) and $\sin 2x$
- [10] Simplify $\sin(x-\pi)$.
- [11] Simplify $\cos(2\pi x)$.
- [12] Find all solutions of $1 + 2\cos x = 0$, where $0 \le x \le 2\pi$.
- [13] Find all solutions of $\sin 2x = -\frac{\sqrt{3}}{2}$.

[14] Sketch the general shape and position of the following graphs. Do not worry about specific x - and y - coordinates.

$$y = x^{5} y = x^{-4} y = x^{3}$$

$$y = e^{x} y = 0.5^{x} y = \log_{0.4} x$$

$$y = \sin x y = \cos x y = \tan x$$

$$4x^{2} + 4y^{2} = 36 4x^{2} + 9y^{2} = 36 4y^{2} - x^{2} = 36 4y^{2} - x = 36$$

[15] Write the series $\frac{3}{2^2 \cdot 4^0} - \frac{4}{3^2 \cdot 4^1} + \frac{5}{4^2 \cdot 4^2} - \frac{6}{5^2 \cdot 4^3} + \frac{7}{6^2 \cdot 4^4} - \frac{8}{7^2 \cdot 4^5}$ in sigma notation with a lower limit of summation of 1.

[16] Simplify
$$\frac{(2n-1)!}{(2n+1)!}$$

[17] Sketch the curve defined by the parametric equations $\begin{aligned} x &= 2t - t^2 \\ y &= t^2 + 2 \end{aligned}$ for $-1 \le t \le 2$ by plotting points.

[18] Find
$$\frac{d^3}{dx^3} \arcsin x$$
.

[19] Find
$$\frac{d^3}{dx^3} \cot^2 x$$
.

[20] If $f'(x) = (1-x)(2+x)^3(3-x)^2$, determine the intervals over which f is decreasing.

[21] Determine if
$$\int_{0}^{\infty} te^{-2t} dt$$
 converges or diverges. If it converges, find its value.

[22] Determine if
$$\int_{2}^{\infty} \frac{1}{x \ln x} dx$$
 converges or diverges. If it converges, find its value

From your calculus textbook:

Section 2.2 29-37 Section 2.5 25-32 Section 2.6 15-24, 28-37 Section 3. Review 1-50 excluding implicit and hyperbolic Section 3.10 1-6 Section 4.4 5-45 Section 4.9 1 - 205, 9, 13, 19, 49, 51 Section 7.8 Section 7. Review 1, 3, 4, 9, 41, 43, 71